Shunt Active Power Filter Based on Instantaneous Power (P-Q) Scheme

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Abstract

Non-linear load which change current and voltage waveform of power system this cases generate harmonics in transmission system. Three-phase six-pulse uncontrolled rectifier is the simple factor in transmission system. This paper presents a study and reduction of source current harmonics in three phase uncontrolled rectifier using instantaneous power scheme based active power filter. This filter also improve power factor. Results are achieved by computer simulation.

Keywords- Active power filter (APF), uncontrolled rectifier, instantaneous power (p-q) scheme, Power factor (PF), THD, Nonlinear load

I. INTRODUCTION

Growing use of power converters and non-linear load which change current and voltage waveform of power system this cases produce harmonics in transmission system. Harmonic is factor of a sine wave with a periodic quantity which the frequency of this is integer Multiple of the Fundamental wave. Harmonic In a power system Cause losses and drop in the transmission and distribution apparatus and power consumption so study and their reduction are necessary. Active power filter is the most efficient way to compensate reactive power and reduces low order harmonics generated by nonlinear load and it also provides power factor improvement as well as adjustment. Three-phase six-pulse diode converters are the simple element in transmission system. These converters because of their nonlinear Properties generate harmonic currents cause thoughtful problems in system.

The RMS value of the nth harmonic of input current

$$I_n = \frac{2\sqrt{2}I_a}{n\pi}\sin\frac{n\pi}{3}\tag{1}$$

The total RMS value of current is

$$I_{rms} = (I_{1(rms)}^2 + I_{2(rms)}^2 + I_{3(rms)}^2 + \dots + I_{n(rms)}^2)^{1/2}$$
 (2)

Input current in the system is

$$i_{a} = \frac{2\sqrt{3}}{\pi} I_{d} \begin{bmatrix} \sin(\omega t - \phi_{1}) + \frac{1}{5} \sin 5(\omega t - \phi_{1}) \\ -\frac{1}{7} \sin 7(\omega t - \phi_{1}) + \frac{1}{11} \sin 11(\omega t - \phi_{1}) - \dots \end{bmatrix}$$
(3)

Where ϕ_1 is phase angle between source voltage and mean current.

Total harmonic distortion is defined as the ratio of the rms value of all harmonic factors to the rms value of the fundamental frequency:

$$THD = \frac{\sqrt{\sum_{k=2}^{\infty} i_{krms}^2}}{I_{1,\dots, \infty}} \tag{4}$$

For a k-pulse ideal rectifier, the harmonics being generated are of orders 5, 7, 11, 13, 17, 19 ..., i.e. those of orders $6k \pm 1$, where k is an integer

II. SHUNT ACTIVE POWER FILTER

Simple circuit arrange of shunt active filter in a three phase, three wire system shown in Figure. This is one of the best fundamental active filters intended for harmonic current compensation of a nonlinear load.

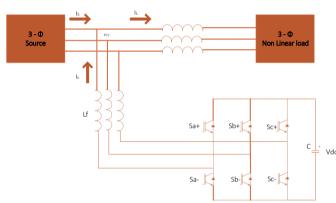


Figure.1 Principle of Current Harmonic Compensation

This shunt active filter equipped with a current minor loop is controlled to draw the Compensating current i_c from the ac power source, so that it cancels the harmonic current contained in the load current i_L [2].

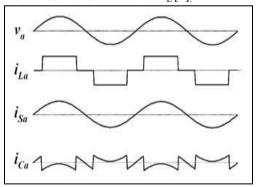


Figure.2 Waveform of Voltage and Current

Figure shows voltage and current waveform of the ac power source V_a , the source current i_{Sa} , and the compensating current i_{Ca} in the a phase, under the following assumption. The smoothing reactor L_{dc} in the dc side of the rectifier large enough to keep constant dc current, the active filter operates as an ideal controllable current source, and the inductor is equal to zero [2].

The shunt active filter should be useful to a nonlinear load that can be considered as a harmonic current

source, such as a diode/thyristor rectifier with an inductive load, an arc furnace and so on. At present, a voltage source PWM converter is generally preferred as the power circuit of the active filter, instead of a current source PWM converter. A main reason insulated gate bipolar transistor, which is one of the most popular power switching strategies, is integrated with a freewheeling diode, so that such an IGBT is much more cost effective in building the voltage source PWM converter than the current source PWM converter. Another reason is that the dc capacitor indispensable for the voltage source PWM converter more compressed and less heavy than the dc inductor for current source PWM inverter [2].

The main purpose of active filter is draw reactive and distortion power to nonlinear load. This can be also shown by the form of currents. On the base of Kirchhoff's law for each phase is filter current given as [3]:

$$i_F(t) = i_L(t) - i_S(t)$$

According to Fourier's analysis distorted periodic function (non-harmonic current of load) can be given by sum of sinusoidal functions that's sum of harmonics, after load current is:

$$i_L(t) = I_0 + \sum_{i=1}^n I_{mi} \sin(i \cdot \omega t - \varphi_i)$$

 $\begin{aligned} Where, &I_0 = DC \ factor \ of \ current \ (we \ will \ not \\ consider \ it), &I_{mi} = amplitude \ of \ i^{th} \ harmonic, \ i = harmonic \\ order \ and \ \phi_i = phase \ angle \ of \ i^{th} \ harmonic. \end{aligned}$

So, we can consider for line current

$$i_{\scriptscriptstyle S}(t) = I_{\scriptscriptstyle m1A} \sin(\omega t)$$

Where, $I_{ml\,A}=$ the amplitude of active part of current fundamental factor.

Current defined is in phase with voltage providing sinusoidal line voltage. That means no phase shift between voltage and current.

After that compensating current of filter is

$$i_F(t) = -I_{m1R} \sin\left(\omega t - \frac{\pi}{2}\right) + \sum_{i=2}^n I_{mi} \sin(i \cdot \omega t - \varphi_i)$$

Where, I_{m1R} = the amplitude of reactive part of current fundamental factor.

This current representation has physical background. From the power representation, first factor of present's reactive power of fundamental factor and second distortion power.

III. PQ SCHEME

The scheme of the Instantaneous Reactive Power in Three-Phase Circuits known as instantaneous power scheme or p-q scheme. It is based on instantaneous values in three-phase power systems with or without neutral wire, and is valid for steady-state or transitory operations, as well as for generic voltage and current waveforms. The p-q scheme consists of an algebraic transformation or clarke transformation of the three-phase voltages and currents in the a-b-c coordinates to the a-B-0 coordinates, followed by the calculation of the p-q scheme instantaneous power factors [4].

Using this transformation we achieve for a voltage system:

$$\begin{bmatrix} v_{\alpha}(t) \\ v_{\beta}(t) \\ v_{0}(t) \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & -\frac{\sqrt{3}}{2} & \frac{\sqrt{3}}{2} \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{bmatrix} \begin{bmatrix} v_{a}(t) \\ v_{b}(t) \\ v_{c}(t) \end{bmatrix}$$

For current

$$\begin{bmatrix} i_{\alpha}(t) \\ i_{\beta}(t) \\ i_{0}(t) \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & -\frac{\sqrt{3}}{2} & \frac{\sqrt{3}}{2} \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{bmatrix} \begin{bmatrix} i_{a}(t) \\ i_{b}(t) \\ i_{c}(t) \end{bmatrix}$$

On the base of instantaneous α - β factors we can define "instantaneous active and reactive power" by following equations:

$$\begin{bmatrix} \mathbf{p}(t) \\ \mathbf{q}(t) \end{bmatrix} = \begin{bmatrix} \mathbf{v}_{\alpha}(t) & \mathbf{v}_{\beta}(t) \\ -\mathbf{v}_{\beta}(t) & \mathbf{v}_{\alpha}(t) \end{bmatrix} \begin{bmatrix} \mathbf{i}_{\alpha}(t) \\ \mathbf{i}_{\beta}(t) \end{bmatrix}$$

So that,

$$p(t) = v_{\alpha}(t) \cdot i_{\alpha}(t) + v_{\beta}(t) \cdot i_{\beta}(t)$$
$$q(t) = v_{\beta}(t) \cdot i_{\alpha}(t) - v_{\alpha}(t) \cdot i_{\beta}(t)$$

IV. COTROL STRATEGY

Reference is the main part of APF control. In fig is shown APF reference current calculation. The calculation is based on p-q scheme. Inputs of the calculation are phase voltages (v_a, v_b, v_c) and phase load currents (i_{La}, i_{Lb}, i_{Lc}) . After transformation (abc to $\alpha\beta$), the $\alpha\beta$ factors of voltage and load current are the inputs of the block of instantaneous active and reactive power calculation defined by pg scheme. Shunt APF should inject to the nonlinear load current which consists of every harmonics beyond active part of fundamental current factor. The easier method to obtain reference current is based on calculation of active part of fundamental current factor which will be after subtracted from load current To obtaining only DC part of instantaneous active power p(t) is desirable to use low pass filter. We can use multiplication by zero for instantaneous imaginary power q(t) filtering. Back transformation for $\alpha\beta$ current factors is given by the following equation [3].

$$\begin{bmatrix} i_{\alpha ref} * \\ i_{\beta ref} * \end{bmatrix} = \frac{1}{v_{\alpha}^2 + v_{\beta}^2} \begin{bmatrix} v_{\alpha} & v_{\beta} \\ v_{\beta} & -v_{\alpha} \end{bmatrix} \begin{bmatrix} p_{DC} \\ 0 \end{bmatrix}$$

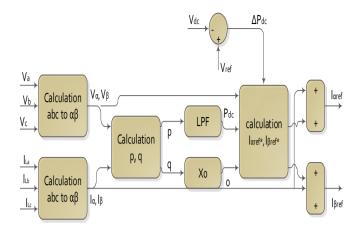


Figure.3 Reference current calculation

The inputs of back transformation will be only the DC part of instantaneous active power and $\alpha\beta$ factors of voltage. By the back transformation we will obtain $\alpha\beta$ factors of active part of current fundamental factor. Complete reference current factors can be obtained by addition $\alpha\beta$ current fundamental factors and $\alpha\beta$ load current factors. For completeness' sake of reference current calculation is necessary to consider the DC bus voltage control keeping constant voltage on capacitor. Charging and discharging of capacitor is ensured by active power flow, in this case represented by active part of current fundamental factor. For DC bus control is used PI controller. Value from the output of PI controller ΔP_{dc} is added to value of DC factor P_{DC} of instantaneous active power [3].

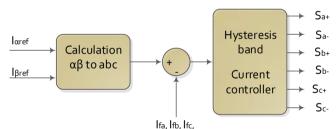


Figure.4 Control Strategy after Reference Current Calculation

Reference current in $\alpha\beta$ coordinates is transferred by inverse transformation ($\alpha\beta$ to abc) to abc reference frame. The hysteresis-band controller is used for the current control. The reference current wave is compared with the actual phase filter current wave. As the error exceeds a prescribed hysteresis band, the upper switch is turned off and the lower switch is turned on. As a results, the output voltage transitions from 0.5 to -0.5 V and the current starts decay. As the error crosses the lower band limit, the lower switch is turned off and the upper switch is turned on [3].

$$\begin{bmatrix} i_{\alpha ref} * \\ i_{\beta ref} * \end{bmatrix} = \frac{1}{v_{\alpha}^2 + v_{\beta}^2} \begin{bmatrix} v_{\alpha} & v_{\beta} \\ v_{\beta} & -v_{\alpha} \end{bmatrix} \begin{bmatrix} p_{DC} \\ 0 \end{bmatrix}$$
 (16)

V. SIMULATION RESULTS

Simulation result is done using MATLAB/Simulink. Figure shows the Simulink diagram of shunt active filer with a three phase diode based uncontrolled rectifier load. The diagram consists power circuit having IGBT switches based VSI inverter with dc

link capacitor, three phase controlled rectifier as a load and control block which include pq scheme reference current calculation and switching pulse generation.

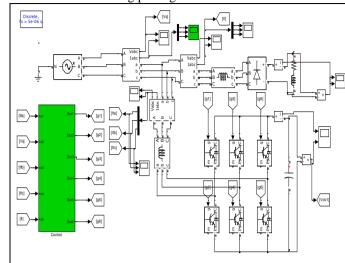


Figure.5 Simulink Diagram of Shunt Active Filter with Controlled Rectifier

Waveform and FFT analysis of Load, Source and Filter Current at load $I_{dc} = 5.934A$

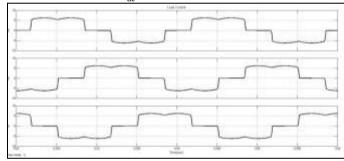


Figure.6 (a) Waveform of Load Current

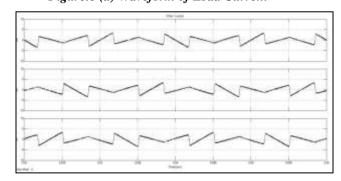


Figure.6 (b) Waveform of Source Current

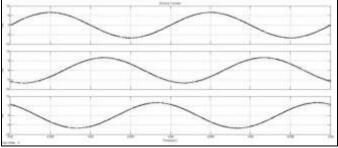


Figure.6 (c) Waveform of Filter Current

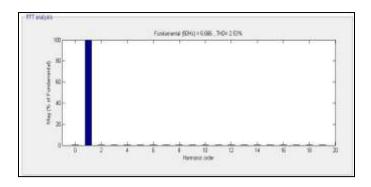


Figure.6 (d) FFT analysis of Source current THD= 2.53%

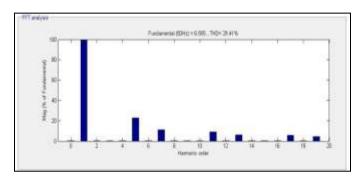


Figure.6 (e) FFT analysis of Load current THD = 29.41%

Table 1. %THD of source and load current with different load current

Load(DC side)			%THD of	%THD of
R (ohm)	L (mH)	Idc	source current	load current
10000	-	0.05942	93.2	30.14
1000	-	0.5941	21.99	30.29
500	-	1.188	11.82	30.14
200	-	2.969	5	29.82
100	50	5.933	2.52	29.32
100	-	5.934	2.56	29.45
100	5	5.934	2.49	29.43
100	10	5.934	2.53	29.41
50	-	11.85	1.56	28.29
50	50	11.85	1.65	28.65

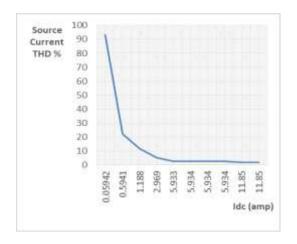


Figure. 7 (a) Source current THD Vs Load Current in amp

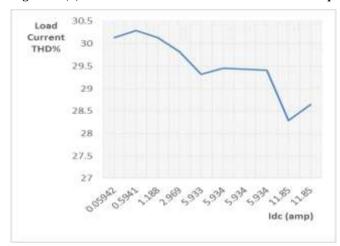


Figure. 7 (b) Load current THD Vs Load Current in amp

VI. CONCLUSION

This paper presents a study and reduction of source current harmonics in three phase uncontrolled rectifier by active power filter based on instantaneous power (P-Q) scheme. Results are achieved by computer simulation

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